

# Integrali indefiniti immediati

- ▶  $\int x^\alpha dx = \frac{x^{\alpha+1}}{\alpha+1} + c$  per  $\alpha \neq -1$  ( $x > 0$  se  $\alpha$  non è intero)
- ▶  $\int \frac{1}{x} dx = \log|x|$  ( $x \neq 0$ )
- ▶  $\int a^x dx = a^x \log_a e + c$  ( $a > 0$ )
- ▶  $\int e^x dx = e^x + c$
- ▶  $\int \cos x dx = \sin x + c$
- ▶  $\int \sin x dx = -\cos x + c$
- ▶  $\int \frac{1}{\cos^2 x} dx = \tan x + c$  ( $x \neq \frac{\pi}{2} + k\pi, k \in \mathbb{Z}$ )
- ▶  $\int \frac{1}{\sin^2 x} dx = -\cotan x + c$  ( $x \neq k\pi, k \in \mathbb{Z}$ )
- ▶  $\int \cosh x dx = \sinh x + c$
- ▶  $\int \sinh x dx = \cosh x + c$
- ▶  $\int \frac{1}{\cosh^x} dx = \tanh x + c$
- ▶  $\int \frac{1}{\sqrt{1-x^2}} dx = \arcsin x + c = -\arccos x + c'$   
 $(-1 \leq x \leq 1; c' = c + \frac{\pi}{2})$
- ▶  $\int \frac{1}{1+x^2} dx = \arctan x + c$  ( $c' = c + \frac{\pi}{2}$ )

# Esercizi - Integrali riconducibili a integrali immediati

1.  $\int (x^2 + x + 3) dx$

2.  $\int \frac{1}{x^4} dx$

3.  $\int x^2 \sqrt{x} dx$

4.  $\int \frac{x^3+x^2+x}{x^2} dx$

5.  $\int \frac{1}{x-1} dx$

6.  $\int \frac{1}{x^2+4} dx$

7.  $\int e^{3x} dx$

8.  $\int \cos 2x dx$

9.  $\int \frac{x+2}{x^2+4x+8} dx$

10.  $\int \sin 4x dx$

## Esercizi - Integrali riconducibili a integrali immediati

$$11. \int \frac{1}{\sqrt{x+3}} dx$$

$$12. \int \frac{x}{\sqrt{4+x^2}} dx$$

$$13. \int \frac{\arcsin^2 x}{\sqrt{1-x^2}} dx$$

$$14. \int \frac{1}{x \log x} dx$$

$$15. \int \frac{e^x}{e^x+3} dx$$

$$16. \int (2x+1)^8 dx$$

$$17. \int \frac{1}{\sqrt{2x-1}} dx$$

$$18. \int \sin^2 x dx$$

$$19. \int \cos^2 x dx$$

$$20. \int \frac{1}{1+\cos x} dx$$

## Esercizi - Integrali riconducibili a integrali immediati

$$21. \int \left( \frac{x^2}{\sqrt{x}} - \frac{1}{x^2} + \sqrt[5]{x} + 2 \right) dx$$

$$22. \int \frac{\cos^3(x)+5}{\cos^2(x)} dx$$

$$23. \int \frac{x^2-1}{x^2+1} dx$$

$$24. \int xe^{-x^2} dx$$

$$25. \int (2x - 3)^3 dx$$

$$26. \int \sqrt[4]{(x - 2)^3} dx$$

$$27. \int x^2 \cos(x^3) dx$$

$$28. \int \cos(x) \sin^4(x) dx$$

$$29. \int \frac{x}{1+x^2} dx$$

## Esercizi - Integrali riconducibili a integrali immediati

$$30. \int \left( \frac{2x}{\sqrt{1+x^2}} \right) dx$$

$$31. \int \frac{1-\cos(x)}{\sin^2(x)} dx$$

$$32. \int \sin(x)e^{\cos(x)} dx$$

$$33. \int \frac{e^x}{e^x+1} dx$$

$$34. \int \frac{1}{e^x+3} dx$$

$$35. \int \frac{(x+1)^2}{x^3} dx \quad \text{sull'intervallo } I = (0, +\infty)$$

$$36. \int \sqrt{\frac{1-x}{1+x}} dx \quad \text{sull'intervallo } (-1, 1)$$

$$37. \int \sin^3(x) dx$$

## Esercizi - Integrali riconducibili a integrali immediati

Ricordiamo

$$\begin{aligned}\cos(\alpha + \beta) &= \cos(\alpha)\cos(\beta) - \sin(\alpha)\sin(\beta), \\ \cos(\alpha - \beta) &= \cos(\alpha)\cos(\beta) + \sin(\alpha)\sin(\beta).\end{aligned}$$

quindi

$$\sin(\alpha)\sin(\beta) = \frac{1}{2} (\cos(\alpha - \beta) - \cos(\alpha + \beta))$$

38.  $\int \sin(2x)\sin(5x) dx$

39.  $\int \frac{3\sin^2(x)}{2+2\cos(x)} dx$  sull'intervallo  $[0, \pi/2]$ .

40. Sia  $f$  la primitiva di  $g(x) = \frac{e^x}{\cosh(x)}$  tale che  $f(0) = \ln(2)$ . Calcolare  $f(\ln(2))$ .

## Esercizi - Integrali riconducibili a integrali immediati

$$41. \int_0^{\frac{\pi}{2}} |\sin x - \cos x| dx$$

$$42. \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 2 \sin x \cos x dx$$

$$43. \lim_{x \rightarrow 0} \frac{5 \int_0^x (e^{-t^2} - \cos^2 t) dt}{x^5}$$

$$44. \int_0^{\frac{\pi}{2}} \sin^3 x \cos^2 x dx$$

$$45. \int_1^2 \frac{x+2}{x^{\frac{5}{2}}} dx$$

$$46. \int_0^1 \left( 2x^{\frac{4}{3}} - \frac{4}{1+3x^2} + \sin 5x \right) dx$$

$$47. \int_0^{\frac{\pi}{2}} \frac{\cos^2 x + \sin 2x}{2 \cos x} dx$$

## Esercizi - Integrali riconducibili a integrali immediati

48.  $\int_1^3 \frac{\ln(x)}{x} dx$

49.  $\int_{2/\pi}^{3/\pi} \frac{1}{x^2} \sin\left(\frac{1}{x}\right) dx$

50.  $\int_0^1 \frac{\sin(2x)}{7+\sin^2(x)} dx$

51. Calcolare l'area  $A$  compresa tra i grafici delle funzioni  
 $f(x) = x^2 - 2x + 1$ ,  $g(x) = x + 1$ .

52.  $\int_1^4 |2-x| dx$

53.  $\int_{\pi}^{\frac{3}{2}\pi} \sqrt{1+\cos(x)} dx$